# **Chapter Number**

# Simplified Analyses of Dynamic Pile Response Subjected to Soil Liquefaction and Lateral Spread Effects

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## 8 1. Introduction

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9 Pore water pressures greater than effective soil stress and subsequent liquefaction are 10 known to occur in saturated sand deposits subjected to earthquake excitations. Liquefaction 11 of soils can result in a reduction of soil strength and yields large settlement via lateral 12 spreading. For superstructures supported on pile foundations embedded in such soils, 13 these effects can be devastating. For example, the 1964 Niigata earthquake in Japan 14 damaged the foundation piles under one of the piers of the 12 spans, 207 meter long 15 Showa Bridge. After the earthquake, an excavation survey of damaged piles indicated that bending failure occurred due to the lateral opreading of river bed soils (Hamada, 1992). 16 17 Similarly, in the 1994, when Northridge earthquake occurs, river bank areas between 18 Santa Clarita and Fillmore, Highway 23 crosses over the Santa Clara River, where sand 19 boils were observed near a bridge pier. Cracks induced by lateral spreading were found 20 approximately 4.5 m away from the pier (Stephen et al., 2002). Afterward, in the 1995 21 Kobe Earthquake, quay walls along the coastline of Kobe moved up to several meters 22 toward the sea as a result of lateral spreading (Tokimatsu and Asaka, 1998). Beside, some 23 papers also discuss even that in long-span bridges under spatially-varying ground 24 motions would suffer liquefaction-induced lateral spread (Abbas and Manohar 2002; 25 Zerva and Zervas, 2002; Wang et al., 2004; Zerva 2009). More recent devastating 26 earthquakes such as the March 2011 Tohoku earthquake in Japan and the January 2010 27 Haiti earthquake can be found and reported by EERI (Earthquake Engineering Research 28 Institute) and USGS (United States Geological Survey).

Recent research has focused on understanding the transfer of forces between a pile and the surrounding layered soil during liquefaction (Hamada, 1992; Meyersohn, 1994; Tokimatsu, 2003, Bhatachaya et al., 2002 \cdot 2004; Jefferies and Been, 2006). Excavation surveys by
Hamada (1992) clearly showed that foundation piles are especially susceptible to damage at the interface between liquefied and non-liquefied layers. This observation was also verified by Meyersohn (1994) and Lin et al. (2005) with static numerical techniques.

In terms of static design for pile foundations, the current mechanism of failure assumes that the soil pushes the pile. The Japanese Road Association Code (JRA, 1996) has incorporated

37 this concept. The code advises civil engineers that the non-liquefied layer acts passive

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pressure on the piles and liquefied layer offers thirty percents of overburden pressure when designing piles against bending failure due to lateral spread. Other codes such as USA code (NEHRP, 2000) and Eurocode 8, part 5 (1998) also have specifications about the problem (Bhattacharya et al., 2005). In the other hand, Tokimatsu (2003) investigated that the equivalent earth pressure acting on the pile during liquefaction in shaking table tests can be defined as the seismic passive pressures subtracting the seismic active pressures. This concept was also verified with the centrifuge tests by Haigh and Madabhushi (2005) and Madabhushi et al (2010). In a design process, engineers need the limit states to define the serviceability of members according to the safety of performances to structures (Priestley et al., 1996; Kramer and Algamal, 2001).

- 11 When piles are subjected to lateral spreading, lateral forces are exerted directly on the 12 embedded depth of piles within liquefied layer. There are generally two methods to analyze 13 this phenomenon. The first method is called the "Force-based method". Using an explicit 14 numerical procedure, earth pressure is applied onto the piles based on a viscous flow model 15 (Chaudhuri et al. 1995; Hamada and Wakamatsu, 1998; Lin et al., 2010). In order to 16 effectively use the force-based method, several soil parameters must be known. Also, the 17 force-based method can account for the effect of soil topography. In the second method, 18 known as the "Displacement-based method", observed or computed lateral ground 19 displacements are transmitted by theoretical soil springs on the whole pile system 20 (Tokimastu and Asaka, 1998; Ishihara, 2003; Chang and Lin, 2003; Cubrinovski and Ishihara, 21 2004; Preitely et al., 2006). The second method has several advantages such as being able to 22 choose a soil spring model that matches the complexity of the soil stratum. Also, nonlinear 23 material effects can be considered.
- 23 material effects can be considered ONAL
- This chapter investigates pile response to loading caused by liquefaction using the EQWEAP (Earthquake Wave Equation Analysis for Pile) numerical analysis procedure (Chang and Lin, 2003; Chang and Lin, 2006; Lin et al., 2010). Both a displacement and forced based form of EQWEAP are used. Methodology and case study comparisons with results of these two procedures are presented separately. The chapter ends with a final synthesis of observations and conclusions drawn from the two methods.

## 30 2. Methodology

## 31 **2.1 Brief overview**

32 The Winkler foundation model is often used in analyzing the deformation behaviors of the 33 pile foundations. For solutions of the dynamic Winkler foundation model, or the so-called 34 beam on dynamic Winkler foundation (BDWF) model, the wave equation analysis, initially 35 proposed by Smith (1960), has been suggested for the driven piles. To make the wave 36 equation analysis more accessible at the time-domain, the author (Chang and Yeh, 1999; 37 Chang et al., 2000; Chang and Lin, 2003) has suggested a finite difference solution for the 38 deformations of single piles under superficial loads. Such formulations can be extended for 39 the case where the piles are subjected to seismic ground shaking. Prior to analysis of the pile 40 system shown in Figure 1, the seismic induced free-field excitation behavior of the soil 41 stratum needs to be obtained. A description of the soil stratum behavior during excitation 42 provides a one-dimensional soil amplification solution for the site. For the site of interest,

43 time dependent earthquake records are used with the modified M-O method to calculate the

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dynamic earth pressure coefficients (Zhang et al., 1998). Liquefaction potential at various depths of the site is evaluated for the limited pore water pressure ratio (Tokimatsu and Yoshimi, 1983). and numerical methods such as the finite element method or the mechanical

4 model which models the discrete model of the pile system (Bathe, 1982).



5 6

Fig. 1. Discrete system of the single pile

7 The earthquake motions can be decomposed into vertical and horizontal components. Pore

8 water pressure effects are accounted for using an excess pore water pressure model. Soil 9

deformation, seismic loading, resistance, damping and the inertia forces of the soil relative

10 to time are applied to the pile segments and used to solve for the corresponding pile

11 displacements. Figure 2 shows the layout of the described superposition procedure.



12

13 Fig. 2. Superposition of the free-field analysis and WEA

1 Formulations can be derived from the wave equations of the piles. Analysis of the 2 3 4 5 foundations can be performed assuming unloaded or time dependant sustained loading conditions. With proper boundary conditions at the pile head, interactions of the structural system can be modeled. The above procedure is known as EQWEAP, which mainly

concerns the nonlinear behaviour of liquefied soil induced permanent ground displacement 6

rather than piles. Figure 3 illustrates the flow chart for the EQWEAP



7

8 Fig. 3. Flowchart summarizing the numerical procedures of the analysis

#### 9 2.2 EQWEAP: Displacement-based method

#### 10 2.2.1 Wave equation of pile foundations concerning soil liquefaction

11 To make the wave equation analysis of the deformations of single piles under superficial 12 loads more accessible in the time-domain, several authors (Chang and Yeh, 1999; Chang et 13 al., 2000; Chang and Lin, 2003) have suggested a finite difference solution. Such 14 formulations can be extended to the case where the piles are subjected to seismic ground 15 shaking. Assuming force equilibrium, the governing differential equations of the pile 16 segment exciting laterally can be written as:

17 
$$E_p I_p \frac{\partial^4 u_p(x,t)}{\partial x^4} + \rho_p A_p \frac{\partial^2 u_p(x,t)}{\partial t^2} + P_x \frac{\partial^2 u_p(x,t)}{\partial x^2} + C_s \frac{\partial u(x,t)}{\partial t} + K_s u(x,t) = 0$$
(1)

18 where  $u(=u_p - u_s)$  = relative pile displacements,  $u_p$  = absolute pile displacements,  $u_s$  = the 19 absolute soil displacements,  $E_p$  =Young's modulus of the pile;  $I_p$  = moment of inertia of the 20 pile,  $\rho_p$  = uniform density of the pile,  $A_p$  = cross-section area of the pile;  $P_x$  = superstructure 21 loads,  $C_s$  and  $K_s$  = damping coefficient and stiffness of the soils along the pile, and x is 22 ordinate variable, and t represents for time. For earthquake loading transmitting from the 23 soils, Eq. (1) can be expanded using the central difference formula as shown below:

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$$u_{p}(i,j+1) = \frac{1}{A+C} \begin{bmatrix} -u_{p}(i+2,j) + (4-B)u_{p}(i+1,j) \\ -(6-2A-2B+D)u_{p}(i,j) \\ +(4-B)u_{p}(i-1,j) - u_{p}(i-2,j) \\ -(A-C)u_{p}(i,j-1) + C[u_{s}(i,j+1) - u_{s}(i,j-1)] + Du_{s}(i,j) \end{bmatrix}$$
(2)

2 where 
$$A = \frac{A_p \rho_p \Delta x^4}{E_p I_p \Delta t^2}$$
;  $B = \frac{P_x \Delta x^2}{E_p I_p}$ ;  $C = \frac{C_s \Delta x^4}{2\Delta t E_p I_p}$ ;  $D = \frac{K_s \Delta x^4}{E_p I_p}$ 

3456789 Eq. (2) indicates that the absolute pile displacements under the earthquake excitations can be solved directly from the absolute displacements of the adjacent soil. A major advantage of this method is that the matrix analysis is not required in solving for the pile deformations. One can simply use a free-field analysis to obtain the liquefied soil displacements using the excess pore water pressure model(as described in Section 2.22) and then substitute the displacements into Eq. (2) to obtain the desired solutions. This is similar to those suggested in the multiple-step analysis of the soil-structure interaction 10 problems. In addition, equations describing the lateral excitations of the highest and 11 lowest elements of the pile should be modified using proper boundary conditions listed 12 as follows.

- 13 Top of the pile:
- 14 a. Free head:

15 
$$\frac{P \mathcal{C}}{\partial x^3} = \frac{P}{E_p I_p}; \frac{P}{\partial x^2} = \frac{N}{E_p I_p}; \frac{P}{\partial$$

16 b. Fixed head:

17

$$\frac{\partial^3 y_p(x,t)}{\partial x^3} = \frac{P_t}{E_p I_p}; \frac{\partial y_p(x,t)}{\partial x} = 0$$
(4)

18 At the tip of the pile:

19 
$$\frac{\partial^2 y_p(x,t)}{\partial x^2} = 0; E_p I_p \frac{\partial^3 y_p(x,t)}{\partial x^3} + P_X \frac{\partial y_p(x,t)}{\partial x} = 0$$
(5)

20 where  $M_t$  and  $P_t$  are the external moment and load applied at the pile head. The discrete 21 forms of these equations can be derived with the central difference schemes. Detailed 22 derivations can be found in Lin (2006).

#### 23 2.2.2 Soil stiffness and damping

24 For discrete models of the various soil types (sand, clay, etc.), both of the stress-25 displacement curves (t-z, q-z and p-y equations) and the Novak's dynamic impedance 26 functions are used popularly in practice. The former, which is established empirically from 27 the in situ pile load tests, can be used for substantial load applied slowly. The later, initially

suggested by Novak (1972, 1974 and 1977) for the soils around the piles subjected to small steady-state vibrations, is able to capture the dynamic characteristics of the soil resistances and energy dissipations. Soil displacements close to a pile subjected to dynamic loading are nonlinear (Prakash and Puri, 1988; Nogami et al, 1992; Boulanger et al., 1999; El Naggar and Bently, 2000). El Naggar and Bently (2000) used a nonlinear soil model that incorporated a p-y curve approach to predict dynamic lateral response of piles to soil movement. The computed responses were found compatible with the results of the statnamic pile test. The nonlinear stiffness of the p-y equations is adapted in this investigation. The corresponding soil stiffness is described as below:

10 
$$k_{NL} = \frac{8\pi G_m (1-v)(3-4v) \left[ \left(\frac{r_0}{r_1}\right)^2 + 1 \right]}{\left(\frac{r_0}{r_1}\right)^2 + (3-4v)^2 \left[ \left(\frac{r_0}{r_1}\right)^2 + 1 \right] \ln\left(\frac{r_1}{r_0}\right) - 1}$$
(6)

11 where  $r_0$  is the pile radius,  $r_1$  is the outer radius of the inner zone, v is Poisson's ratio of 12 the soil stratum, and  $G_m$  is the modified shear modulus of the soils. A parametric study 13 shows that a ratio  $r_0 / r_1$  of 1.1-2.0 yields the best agreement.

For the damper, a transformed damping model is used. Equivalent damping ratios, D, of the soils at steady-state excitations are first computed from the Novak's dynamic impedance

16 functions, K\* where 
$$K^* = K_{real} + i K_{imag} = K(\omega) + i \omega C(\omega) = K(\omega) (1 + 2iD)$$
 (7)

18

$$D \cong \frac{\omega C(\omega)}{(2K(\omega))} \tag{8}$$

19 In the above equations,  $K(\omega)$  and  $C(\omega)$  are the frequency-dependent stiffness and damping 20 coefficient of the impedance. For simplicity, the computed damping ratios are incorporated 21 with the static stiffness Kst to model the kinematics of the soil. The revised damping 22 coefficient  $c(\omega)$  can be written as:

$$c(\omega) \cong 2DK_{st} / \omega \tag{9}$$

24 Decomposing the actual load-time history into a series of small impulses, the damping 25 coefficient c(t) can be obtained by integrating a damping function c(t) to a set of unit 26 impulses of the actual load-time history. Knowing that  $D=C(\omega)\omega/2K(\omega)$ , the associated 27 geometric damping ratios can be computed. Modeling the values of  $D(\omega)/\omega$  and assuming 28 that they are symmetric with respect to the ordinate, a mathematical expression of the 29 damping can be written as:

$$30 c(t) = AK_s t^{-B} (10)$$

31 where A and B are the model parameters (Chang and Yeh, 1999; Chang and Lin, 2003).

#### 1 2.2.3 Modeling soil liquefaction

Soils affected by induced pore-water pressure reduce the lateral resistance of the piles. This study utilized an excess pore water empirical model to complete effective stress analysis (Martin et al., 1975; Finn et al, 1977; Finn and Thavaraj, 2001), and obtain free-field motions under liquefaction. Kim (2003) successfully predicted the excess pore-water pressure resulting in soils subjected to earthquake shaking by verifying results with laboratory tests. This model can be divided into undrained conditions and drained conditions as follows:

- 8 a. Undrained condition:
- 9

14

$$\Delta u_w = \frac{\Delta \varepsilon_{vd}}{\left(\frac{1}{\overline{E}_r} + \frac{n_p}{K_w}\right)} \tag{11}$$

10 where  $\Delta u_w$  = an increase in pore water pressure;  $\Delta \varepsilon_{vd}$  = an increment in volumetric strain;

11  $\overline{E}_r$  = one dimensional rebound modulus at an effective stress ( $\sigma'_v$ );  $n_p$  = porosity, and  $K_w$  = 12 bulk modulus of water.

13 For saturated sand 
$$K_w >> \overline{E}_r$$
 and therefore

$$\Delta u_w = \overline{E}_r \Delta \varepsilon_{vd} \tag{12}$$

15 According to simple shear test, the volumetric strain increment ( $\Delta \varepsilon_{vd}$ ) is a function of the total

accumulated volumetric strain (
$$\varepsilon_{S}$$
) and the shear strain ( $\gamma$ ). The relationship is given by

17 
$$\Delta \varepsilon_{vd[i]} = C_1 (\gamma - C_2 \varepsilon_{vd[i-1]}) + \frac{C_3 \varepsilon_{vd[i-1]}^2}{\gamma + C_4 \varepsilon_{vd[i-1]}}$$
(13)

18 
$$\varepsilon_{vd[n]} = \sum_{i=1}^{n} \Delta \varepsilon_{vd[i]}$$
(14)

19 where [i] = ith time step or cycle; and  $C_1$ ,  $C_2$ ,  $C_3$ , and  $C_4$  are constants depending on the

soil type and relative density. An analytical expression for rebound modulus ( $\overline{E}_r$ ) at any effective stress level ( $\sigma'_v$ ) is given by

22 
$$\overline{E}_{r} = \frac{(\sigma_{v}^{'})^{1-m}}{mk_{2}} (\sigma_{v0}^{'})^{m-n}$$
(15)

where  $\sigma'_{v0}$  is initial value of the effective stress; and  $k_2$ , *m* and *n* are experimental constants for the given sand.

25 b. Drained condition:

If the saturated sand layer can drain during liquefaction, there will be simultaneous
generation and dissipation of pore water pressure (Sneddon, 1957; Finn et al. 1977). Thus,
the distribution of pore-water pressure at time (t) is given by

1

5

$$\frac{\partial u_w}{\partial t} = \overline{E}_r \frac{\partial}{\partial z} \left( \frac{k}{r_w} \frac{\partial u}{\partial z} \right) + \overline{E}_r \frac{\partial \varepsilon_{vd}}{\partial t}$$
(16)

2 where u = the pore-water pressure; z = the corresponding depth; and k = the permeability ; 3 and  $r_w$  is the unit weight of water. Before conducting the free-field analysis, the adequate 4 shear modulus (Seed and Idriss, 1970) may be determined from the following equation

$$G = 1000K_2(\sigma'_m)^{0.5} \tag{17}$$

6 where  $K_2$  is a parameter that varies with shear strain and  $\sigma'_m$  is the mean effective stress. 7 Pore water pressure will increase during shaking and leads to a decrease of effective stress. 8 In some situations, pore-water pressure equals overburden stress in sand deposits and may 9 liquefy. The initial shear modulus can be calculated from the initial effective stress. Then, *G* 10 is modified due to the shear strain and pore water pressure under liquefaction. The 11 modified value is substituted in place of the former one and convergence of solutions is 12 obtained using an iterative manner.

13 In addition, to avoid over-predicting the excess pore water pressure and ensure 14 compatibility with practical observations, it is suggested to use the pore water pressure ratio 15  $(r_u)$  to accurately control soil liquefaction levels (Lee and Albaisa, 1974; DeAlba et al., 1976;

16 Tokimatsu and Yoshimi, 1983). The equation is given by

17 
$$Persol field F_{L}^{\frac{1}{\alpha\beta}} = 0 py$$
(18)

18 where  $\alpha$ ,  $\beta$  are the experienced constants, and  $F_L$  is the safety factor of liquefaction. In 19 order to use the above formulas, the liquefaction potential analysis of the site needs to be 20 conducted prior to the analysis.

#### 21 2.2.4 Free field analysis

22 The one-dimensional seismic excitations of soils onto the piles are computed from a free-23 field response analysis for the site of interest. Such an analysis can be conducted using the 24 finite element technique, or be simply solved for using the 1-D wave propagation model and 25 the lumped mass analysis. For simplicity, the lumped mass model is selected. To analyze the 26 equations of motion of the soil layer under the earthquake excitations, the relative 27 deformations of the structural system are obtained with the base accelerations induced by 28 the earthquake. Base motions of the site are obtained by modifying the seismic accelerogram 29 recorded at the ground surface of that site. This is done simply by obtaining the frequency-30 spectrum of the accelerogram, and then multiplying it with the analytical 'transfer function' 31 represented for the ratios of the accelerations occurring at the base (bedrock) and those at 32 the ground surface of that site (Roesset, 1977). This computation would complete a 33 frequency-domain convolution and prepare a base-acceleration spectrum to solve for the 34 corresponding accelerogram. To have consistent results for a specific site, one must be very 35 cautionous about the wave velocities and the thickness of the soil layers used in the 36 analyses. Crosschecks are required for vertical and horizontal excitations to ensure that the

- 1 2 3 analytic parameters are rational. Notice that the discrete solutions of the wave equations are
- in terms of the displacements only. To obtain the time-displacement history of the soils, a
- baseline correction procedure (Kramer, 1996) is suggested to eliminate the integral offsets of the velocities and displacements appearing after the quake excitations. The responses of the
- free-field using the above procedure have been checked with the solutions of FEM as shown
- 4 5 6 in Figure 4. Using this simplified model just be only computed one-way ground response
- 7 depending on the inputted seismic motions. And, despite the simplicity of the geometry, an
- 8 exact solution of the full model, and a detailed analysis of the phenomenon, have not
- 9 perfectly been achieve (Schanz and Cheng, 2000).



## 10

11 Fig. 4. Comparison of numerical results from WEA and FEM

#### 12 2.3 EQWEAP: Force-based method

#### 13 2.3.1 Wave equation of pile foundations concerning lateral spread

14 The wave equation describing a single pile under lateral loads can be derived based on a 15 force equilibrium of the pile segments shown in Figure 1 as follows,

16 
$$EI\frac{\partial^4 u(x,t)}{\partial x^4} + \rho A \frac{\partial^2 u(x,t)}{\partial t^2} + P_x \cdot \frac{\partial^2 u(x,t)}{\partial x^2} = P(x,t)$$
(19)

17 where u is the lateral pile displacement relative to the soil, E is the Young's modulus of the 18 pile, I is the moment inertia of the pile,  $\rho$  is mass density of the pile, A is the cross-sectional 19 area of the pile,  $P_x$  are the superstructure loads, P(x,t) is the time-dependent loading due to 20 laterally spreading at various depths, x is ordinate variable, and t represents for time. Using

21 explicit finite difference schemes, the discrete form of Eq. (19) can be written as

(21)

$$u(i, j+1) = \frac{1}{A_1} \begin{vmatrix} -u(i+2, j) + (4-B_1) \cdot u(i+1, j) \\ +(2A_1+2B_1-6) \cdot u(i, j) \\ +(4-B_1) \cdot u(i-1, j) - u(i-2, j) \\ -A_1 \cdot u(i, j-1) + C_1 \end{vmatrix}$$
(20)

2 where 
$$A_1 = \frac{\rho A \Delta x^4}{E I \Delta t^2}$$
;  $B_1 = \frac{P_x \Delta x^2}{E I}$ ;  $\frac{P(x,t) \Delta x^4}{E I}$ .

For the initial condition, u(i, j) and u(i, j-1) are set to zero. Equation 20 can only calculate the responses of piles under lateral loads along the lenfth of the pile. The head and tip can not be solved for. With proper boundary conditions (see Eq. 3~4), the other equations can then be derived. While the liquefaction-induced dynamic earthquake pressures are computed, the pile responses at various depths can be solved through the above formulations.

## 8 2.3.2 Dynamic earth pressure

9 Since Okabe (1926) and Mononobe and Matsuo (1929) introduced the concept of dynamic 10 lateral pressure, many reports and practical works have been conducted in this manner 11 (Ishibashi and Fang, 1987; Richard et al., 1990; Ishibahi et al., 1994; Budhu and Al-karni, 12 1993; Richard et al., 1993; Soubra and Regenass, 2000). Tokimatsu (1999, 2003) and Uchida 13 and Tokimatsu (2005) determened several factors that affect the response of a pile in 14 saturated sand by using a shaking table tests. They suggested that the total earth pressure 15 acting on the foundation, when neglecting the triction between foundation and soil (see Fig. 16 5), is define as: 

$$P_E = P_{EP} - P_{EA} = Q - F$$

18 where 
$$P_E$$
 is total earth pressure,  $P_{EP}$  and  $P_{EA}$  are earth pressures on the active and passive

19 sides, *Q* is shear force at the pile head, and *F* is total inertial force from the superstructure



20

21 Fig. 5. Schematic layout of forces acting on Foundation (from Uchida and Tokimatsu, 2005)

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- 1 and foundation. In addition, Haigh and Madabhushi (2005) have verified that the adjacent stresses of single piles subjected to lateral spreading forces would range between the active
- 2 3 state and the passive state through centrifuge modeling.
- 4 Based on the Mononobe-Okabe method, Zhang et al. (1998) successfully derivates the time-5 6 7 dependent coefficients of earth pressure under active and passive states that involves the motions of soils and foundations. One can also modify the plane strain model of soil wedge to extend it to be three dimensional analysis. The descriptions and formulations of the
- 8 coefficients of active and passive earth pressures are referred to Zhang et al. (1998).

#### 9 2.3.3 Modeling lateral spread

10 For lateral spread induced by liquefaction, the soil properties such as the unit weights and 11 the friction angles of the soils could be corrected based on the calculated pore water 12 pressure ratios. There are two ways depicting the weakness of soils during liquefaction 13 (Matsuzawa et al. 1985; Ebeling and Morrison, 1993). Those equations are given by

$$\gamma'_s = \gamma_s (1 - r_u) \tag{22}$$

15 
$$\phi'_{eff} = \tan^{-1}[(1 - r_u)\tan\phi']$$
 (23)

16 where  $\gamma'_s$  is the unit weight of the soil,  $\gamma_s$  is the effective unit weight of the soil,  $\phi'$  is the 17 friction angle of the soil, and  $\phi'_{eff}$  is the effective friction angle of the soil.



19 Fig. 6. Distribution of earth pressure along a pile

Figure 6 illustrates the distributions of earth pressures along the pile with the discrete blocks and nodes. According to the geometry of pile (see figure 7) and Eq. (24), the lateral forces at various depths are determined by

4

$$P_E = (\gamma'_s Z K_E) \cdot (B)$$
(24)

5 where Z is the corresponding depth of node,  $K_E$  is the equivalent dynamic coefficients of

- 6 earth pressure (i.e.  $K_E = K_{EP} K_{EA}$ ), and *B* is the loaded width of the pile body (=  $\pi d / 2$ ,
- 7 where *d* is the pile diameter).



8

9 Fig. 7. The loaded width of the pile body due to lateral spreading

## 10 **3. Practical simulation**

11 In the following section, two case studies are presented, one of which focuses on pile 12 foundation damagess caused by the Niigata earthquake in Japan (Hamada, 1992) and the 13 other which focuses on foundation pile cases damaged during the 1995 Kobe earthquake. 14 The Niigata earthquake case study utilize the displacement-based EQWEAP method, in 15 which the free-field and the wave equation analysis are both performed to calculate the 16 dynamic responses of piles under liquefaction. In The Kobe earthquake case studies, the 17 force-based EQWEAP method is utilized to assume lateral flow induced forces on the piles. 18 Dynamic earth pressures caused by lateral spreading of the liquefied layers are first 19 generated and used to model forces exerted on the piles where the deformations of piles 20 occur. These results show the pile failure pattern validate the applied methodology.

## 21 **3.1 Case study: Pile damages due to soil liquefaction**

The Niigata Family Court House was a four-story building located on the left bank of the Shinano River. The building was supported on a concrete pile foundation (Figure 8) each pile of the foundation having a a diameter of 35 cm and length of 6 to 9m. During the earthquake, the pile foundations were damaged by liquefaction-induced ground displacement. Excavation surveys showed that two piles (No.1 pile and No.2 pile) had severe cracks (Figure 9). They were conjecturally crushed by excessive bending moments at

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the interface between liquefied and non-liquefied layers as shown in Figure 9. According to 1 2 3 4 5 6 7 aerial photographs of the area, the permanent ground displacement in the vicinity of building moved approximately 1.1m and the maximum displacement of No.1 pile and No.2 pile were respectively 50 cm and 70cm. For simplification, the entire soil system could be assumed as an upper layer and a lower layer. The upper layer from the ground surface to the depth of 8m is classified as medium-dense sand. The lower layer from the depth of 8 to

11m is classified as dense sand. The time history of earthquake record adopted the NS-8 component of the 1964 Niigata Earthquake as illustrated in Figure 10.



10 Fig. 8. Footing and foundation beams of Niigata Family Court House (from Hamada, 1992)



11

12 Fig. 9. Damage to piles and SPT-N values in sit u (from Hamada, 1992)

1 2







6 The initial shear modulus of the soils at the any depth can be calculated by Eq. (17). The 7 distribution of shear modulus is similar to the hyperbolic form observed in gibson soils and 8 increases with the depth. The determination of pore water ratio pressure ( $r_u$ ) and reduction 9 factors ( $D_F$ ) versus depth can be estimated by the liquefaction potential method suggested 10 by Tokimatsu and Yoshimi (1983) with Eq. (18) for various levels of liquefaction. Moreover, 11 one can conduct EQWEAP analysis to obtain the liquefied free-field response considering 12 the effect of pore water. The excess pore pressure ratios at different depths are shown in 13 Figure 11. It was found that the soil layer reached a liquefied state gradually after 2.8 14 seconds.

15 Figure 12 shows the time histories of ground motions. The maximum displacement of the 16 ground which takes place at the surface is 47.3 cm at about 10 seconds. The liquefied layer 17  $(r_u = 100\%)$  ranging between the depths of 2 m to 8m displaces by 30 cm to 45 cm (see 18 figure 12). The displacements reduce to about 3 cm below the liquefied layer for 19  $r_{\mu} = 14 \sim 45\%$  as shown in Figure 12. Figure 13 indicate the maximum displacements of 20 piles at various depths from wave equation analysis. Based on the results form Figure 13, 21 the peak value occured at the pile head and the relative displacements between the pile 22 head and pile tip are 50 cm and 69 cm. The maximum bending moments of piles are 23 shown in Figure 14 and those peak values would also occur approximately at the interface 24 between liquefied and non-liquefied layers. Comparing the numerical results by 25 Meryersohn (1994), the computed values are nearly consistent with the ones reported. In 26 the meantime, the peak shear forces of piles also occur at this zone. Therefore, the 27 excessive bending moment and shear zone of the pile is again revealed in this study using 28 the suggested procedures.





Fig. 11. The time history of excess pore pressure ratios at different depths





Fig. 12. Time histories of ground motions at different depths





Fig. 14. Maximum pile bending moments for No.1 Pile and No.2 Pile

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#### 1 3.2 Case study: Pile damages due to lateral spread

2 3 4 5 6 Mikagehama is a man-made island in the port area of Kobe home to a number of liquefied propane gas (LPG) and oil tanks. During the 1995 Kobe Earthquake, the soils underlying the foundatinos of tanks liquefied. A guay wall moved seaward and lateral spreading of the backfill soils damage the piles supporting the tanks. Oil-storage tank TA72 is chosen to be a target, which is located in the west part of the island about 20m from the waterfront. Figure 7 15 illustrates the cross sectional view of tank and underlying pile foundations. The tank has 8 a diameter of 14.95 m and its storage capacity is about 2450 kl. It is supported on 69 precast 9 concrete piles each with the length of 23 to 24 m and diameter of 45 cm. The water table is 10 estimated at the depth of 2 to 3 m. Sand compaction piles were conducted to increase the 11 SPT-N values of the Masado layer around the outside of Tank TA72.

12 According the relation between the bending moment (M) and curvature ( $\varphi$ ) where  $D_0$  is 13 the diameter of pile and N is axial load on pile head, one can know that the cracking 14 bending moment ( $M_{cr}$ ), the yield bending moment ( $M_{u}$ ) and the ultimate bending moment 15  $(M_{\mu})$  are 105 kN-m, 200 kN-m, and 234 kN-m respectively. The ultimate shear strength is 16 232 kN with regards to ACI (1998). Ishihara and Cubrinovski (2004) have utilized bore-hole 17 cameras and inclinometers to inspect the damages of the piles. Their results for pile No. 2 18 are shown in Figure 15. The main failure field was located at depth of 8 to 14 m where the 19 piles were found to have developed many cracks. Moreover, pile No. 2 has scraped wounds 20 due to large deformations where lateral spreading of liquefied soils develops along the 21 weak interface. To quantifying damage in structures under earthquakes in terms of Park and 22 Ang damage indices, which provides a measure on the structure damage level, and making 23 a decision on necessary repair possible, the value approached to be 0.8 to represent collapse 24 state (Park and Ang, 1985; Moustafa, 2011).



26 Fig. 15. Cross sectional view of Tank TA 72 and its foundation (from Ishihara and

1 In this study, the length of pile is assumed to be 24 m with a diameter of 45 cm. Seismic 2 record of the NS-component of 1995 Kobe Earthquake is adopted. According to the field 3 data, distributions of pore water ratio pressure ( $r_u$ ) versus the depths can be estimated by 4 evaluating the liquefaction potential of that site. With all the required data and 5 incorporating with the modified M-O model (Zhang et al, 1998), the dynamic coefficients of 6 earth pressure are computed as shown in Figure 16. Also, the unit weight of the soil is 7 reduced by  $r_{\mu}$  (refer to Eq. 22). When obtaining those dynamic earth forces to insert and 8 execute the wave equation analysis, the time histories of displacements along the pile can be 9 illustrated as shown in Figure 17. The displacement of the pile head oscillates significantly 10 with time, but the peak value is smallest. As the depth increases, the peak displacement of 11 pile becomes larger. Those peak displacements along the pile are shown in Figure 18(a). The 12 maximum value among them occurs at the pile tip about 52.7 cm and the maximum relative 13 displacement between the pile top and the pile bottom is estimated about 44.7 cm. The 14 deformed shape of the pile is similar to pile No. 2. It can be found that the maximum 15 bending moments which exceed the ultimate bending moment at depths of 2 to 23 m and 16 that this zone is the mose dangerous zone.. With regards to the shear failure, the weak 17 interface exists at a depth of 11 m, in which the maximum shear force is close to the ultimate 18 (Figure 18b~18c). The above observations are agreeable to field investigations reported by 19 Ishihara and Cubrinovski (2004).



21 Fig. 16. Dynamic coefficients of earth pressure







Fig. 17. Time histories of lateral displacement along the Tank TA72 No.2 pile



## 4 4. Conclusions

1 2 3

5 EQWEAP is a simplified but effective procedur to analyze the dynamic pile-soil interaction 6 under the earthquake. In the analysis, the pile deformations are obtained solving the 7 8 discrete wave equations of the pile, where the seismic ground motions are pre-calculated from one-dimensional lumped mass model assuming a free-field condition or dynamic earth 9 pressure are directly exerted onto the pile. This chapter presented both displacement- and 10 forced-based form of the EQWEAP analysis method along with two comparative case 11 studies: Using wave equation analysis and the EQWEAP method, pile response to 12 liquefaction has been computed and compared to the case histories of the Niigata 13 earthquake records. Case histories of the Kobe earthquake show that the lateral spreading 14 can be a major cause to damage the piles. Specifically conclusions for the displacement and 15 forced based EQWEAP methods can be summarized as follows:

- Based on the suggested numerical procedure using EQWEAP (Chang and Lin, 2003; Lin et al., 2011), one can evaluate the motions of the soil stratum and the pile foundations at various depths to estimate the occurrence of pile damages and patterns of failure. This procedure provides a simplified but rational dynamic analysis to the pile foundation design work.
- 21 2. The use of the empirical excess pore pressure model for liquefaction can be applicable to soils underneath the liquefiable layers using a minimum pore pressure ratio. The pore pressure ratio should be calculated using the empirical formula suggested by Tokimatsu and Yoshimi (1983) providing that the factors of safety against liquefaction are known.

- 3. Not only the interfaces between the liquefied and non-liquefied layers can exert excessive bending moments and shear stress, but also the layer contrast of the soils can yield similar effects. Engineers need to be more careful in designing pile shafts that are susceptible to fail due the liquefaction resulting from earthquakes and the layer contrast.
- 1 2 3 4 5 6 7 8 9 The wave equation analysis can be used to model the pile responses under lateral 4. spread due to earthquake. The modified M-O model (Zhang et al., 1998) incorporating reduction methods for soil parameters were successfully used to represent the dynamic earth pressures of the lateral spread. The numerically determined pile deformations 10 were similar to deformations discovered at piles actually affected by lateral spread. In 11 advance, if nonlinear behaviour of pile such as the moment-curvature relationship and 12 complexity of pile geometries can also be considered simultaneously in this method, the 13 results would be enhanced to capture detailed mechanism and definite performance of 14 piles foundations.

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